



# Vortex mediated Josephson plasmon bound states

Marios H. Michael

*Max Planck Institute for the Structure and Dynamics of Matter*

**Mathematical aspects of condensed matter physics, ETH 2023**





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# Dissipationless currents in pseudogap YBCO



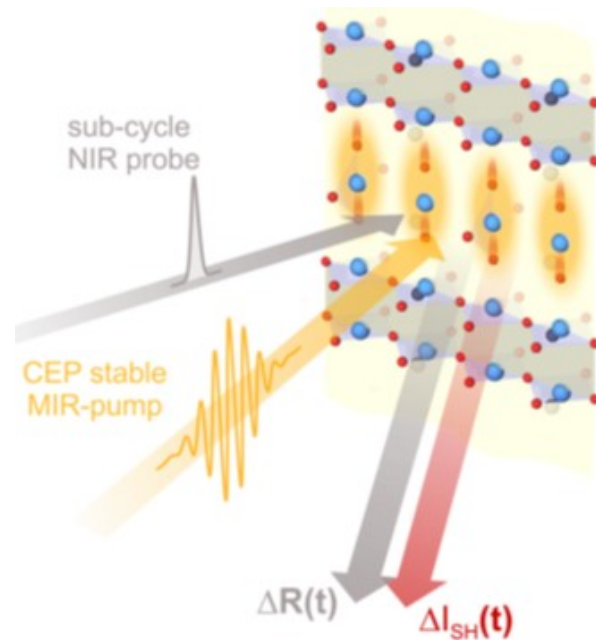
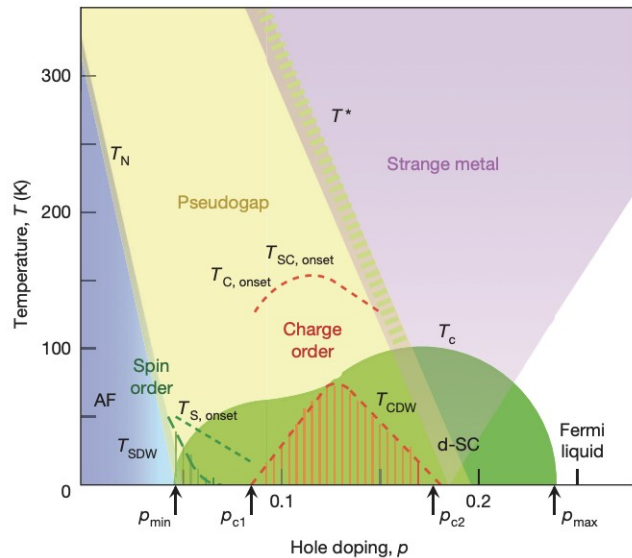
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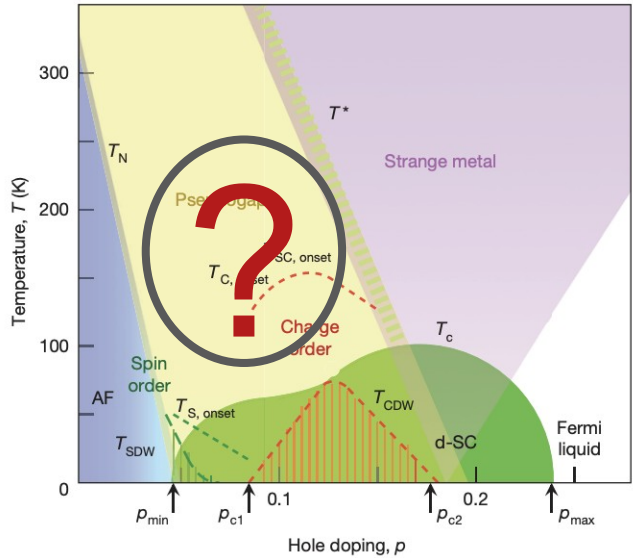


# High $T_c$ cuprates - the pseudogap phase



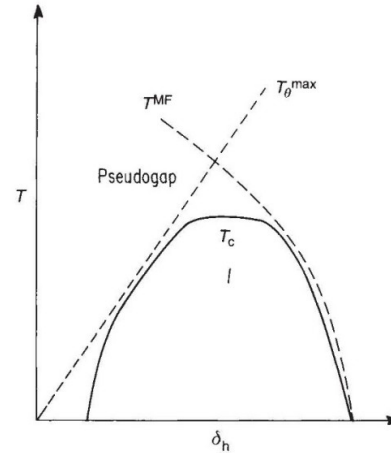
B. Keimer, A. Kivelson et al., Nature (2015)

# High Tc cuprates - the pseudogap phase



B. Keimer, A. Kivelson et al., Nature (2015)

Competition between mean field and phase fluctuation transition:



V. J. Emery & S. A. Kivelson, Nature (1995)

# This talk :

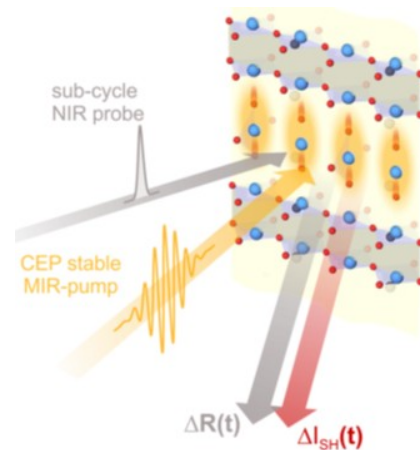
1. Present numerical simulations of the pseudogap phase.
2. Intuition behind the existence of dissipationless counterflow currents in YBCO.
3. Connection with experimental observations in light-driven YBCO. **(references)**

Phys. Rev. B **102**, 174505 M. H. M. et al. (2020)

Phys. Rev. X **12**, 031008 (2022) (2022) Alex von Hoegen

Physical Review B, **89**, 184516 (2014), S. Kaiser et al.

Nature Materials, **13**, 705–711 (2014), W. Hu et al.



# Dissipationless counterflow currents above $T_c$ in bilayer superconductors

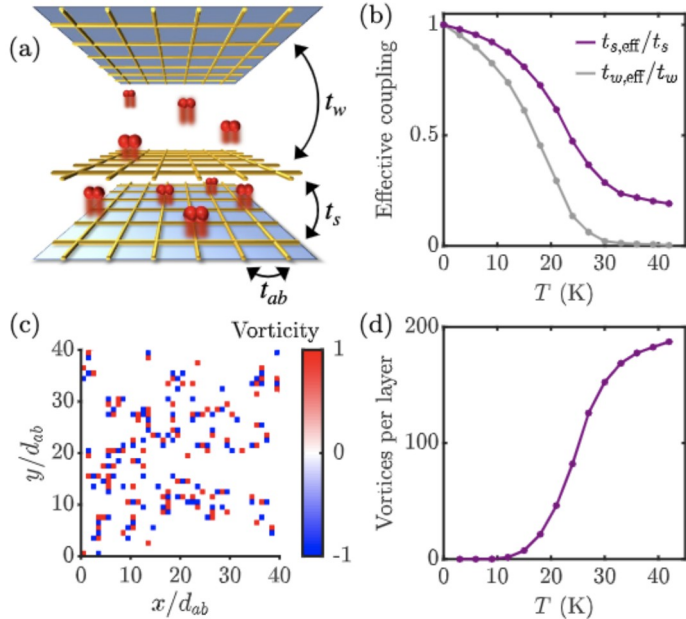
Guido Homann,<sup>1</sup> Marios H. Michael,<sup>2</sup> Jayson G. Cosme,<sup>3</sup> and Ludwig Mathey<sup>1,4</sup>

<sup>1</sup>Zentrum für Optische Quantentechnologien and Institut für Quantenphysik, Universität Hamburg, 22761 Hamburg, Germany

<sup>2</sup>Max Planck Institute for the Structure and Dynamics of Matter,  
Luruper Chaussee 149, 22761 Hamburg, Germany

<sup>3</sup>National Institute of Physics, University of the Philippines, Diliman, Quezon City 1101, Philippines

<sup>4</sup>The Hamburg Centre for Ultrafast Imaging, Luruper Chaussee 149, 22761 Hamburg, Germany



Guido Homann

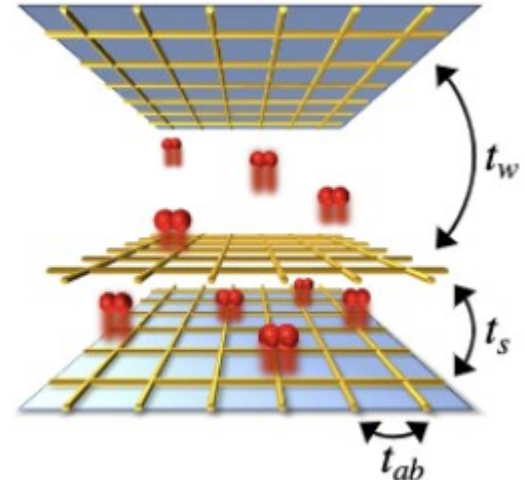
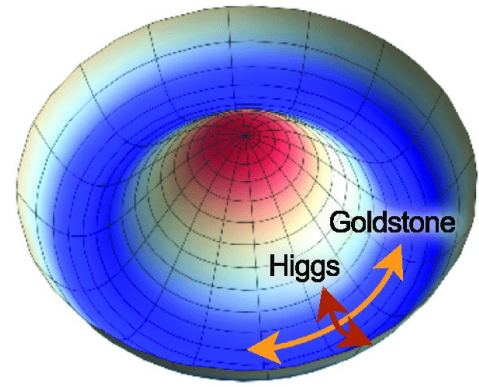
to appear on arXiv soon...

# Theory of pseudogap YBCO: U(1) gauge invariant bilayer model

Superconducting potential:

$$\mathcal{L}_{\text{SC}} = \sum_{\mathbf{r}} K \hbar^2 |\partial_t \psi_{\mathbf{r}}|^2 + \mu |\psi_{\mathbf{r}}|^2 - \frac{g}{2} |\psi_{\mathbf{r}}|^4$$

Mexican hat potential





# Theory of pseudogap YBCO: U(1) gauge invariant bilayer model

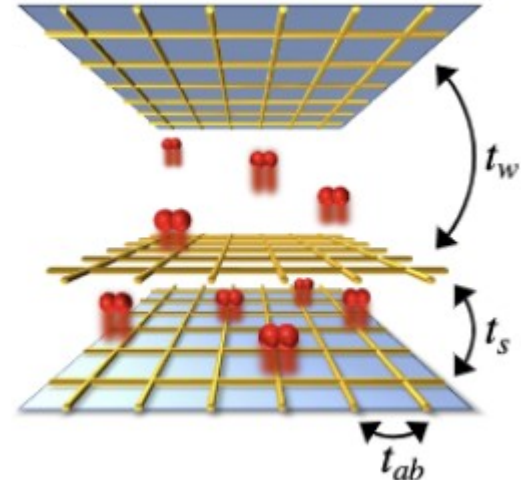
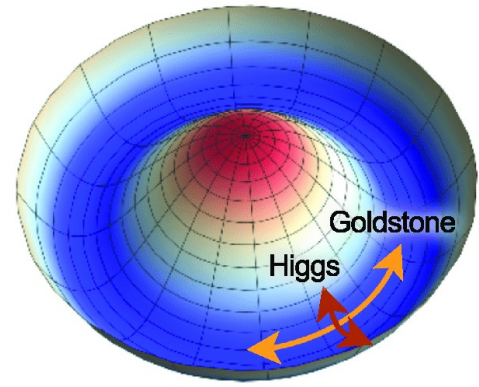
Superconducting potential:

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Tunneling of cooper pairs:

$$\mathcal{L}_{\text{kin}} = - \sum_{j, \mathbf{r}} t_{j, \mathbf{r}} |\psi_{\mathbf{r} + \mathbf{u}_j} - \psi_{\mathbf{r}} e^{i a_{j, \mathbf{r}}} |^2.$$

Bilayer anisotropic 3D XY-model



# Theory of pseudogap YBCO: U(1) gauge invariant bilayer model

Superconducting potential:

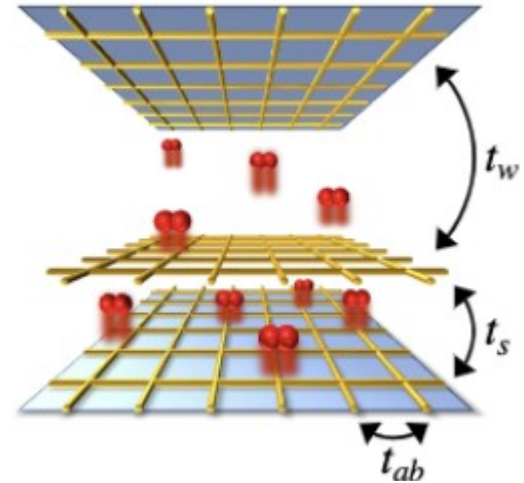
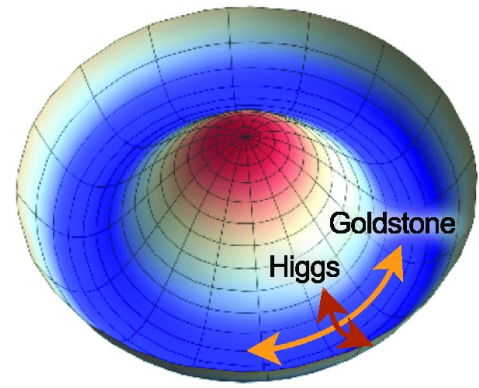
$$\mathcal{L}_{\text{sc}} = \sum_{\mathbf{r}} K \hbar^2 |\partial_t \psi_{\mathbf{r}}|^2 + \mu |\psi_{\mathbf{r}}|^2 - \frac{g}{2} |\psi_{\mathbf{r}}|^4$$

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Maxwell Hamiltonian:

$$\mathcal{L}_{\text{em}} = \sum_{j, \mathbf{r}} \frac{\kappa_{j, \mathbf{r}} \epsilon_{\infty} \epsilon_0}{2} E_{j, \mathbf{r}}^2 - \frac{\kappa_{z, \mathbf{r}}}{\kappa_{j, \mathbf{r}} \beta_{j, \mathbf{r}}^2 \mu_0} \left[ 1 - \cos(\beta_{j, \mathbf{r}} B_{j, \mathbf{r}}) \right]$$

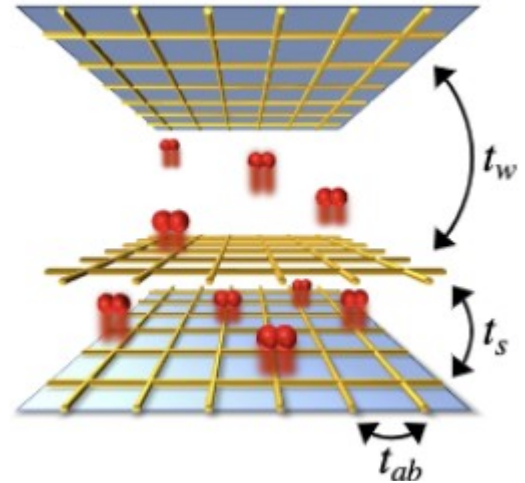


Coupling to light

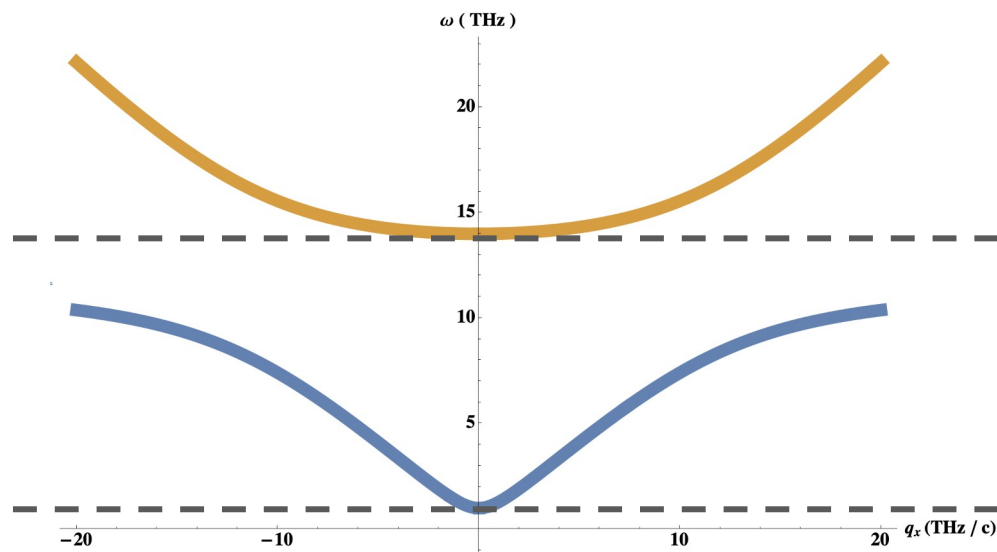
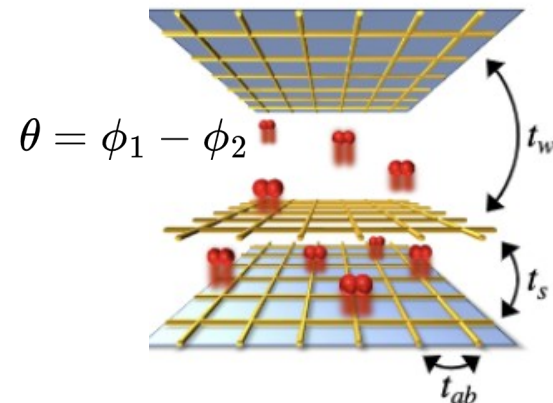
# Theory of pseudogap YBCO: **U(1) gauge invariant bilayer model**

Semi-classical Langevin dynamics:

$$\partial_t^2 \psi_{\mathbf{r}} = \frac{1}{K \hbar^2} \frac{\partial \mathcal{L}}{\partial \psi_{\mathbf{r}}^*} - \gamma_{\text{sc}} \partial_t \psi_{\mathbf{r}} + \xi_{\mathbf{r}},$$
$$\partial_t^2 A_{j,\mathbf{r}} = \frac{1}{\epsilon_{\infty} \epsilon_0} \frac{\partial \mathcal{L}}{\partial A_{j,\mathbf{r}}} - \gamma_{j,\mathbf{r}} \partial_t A_{j,\mathbf{r}} + \eta_{j,\mathbf{r}}$$



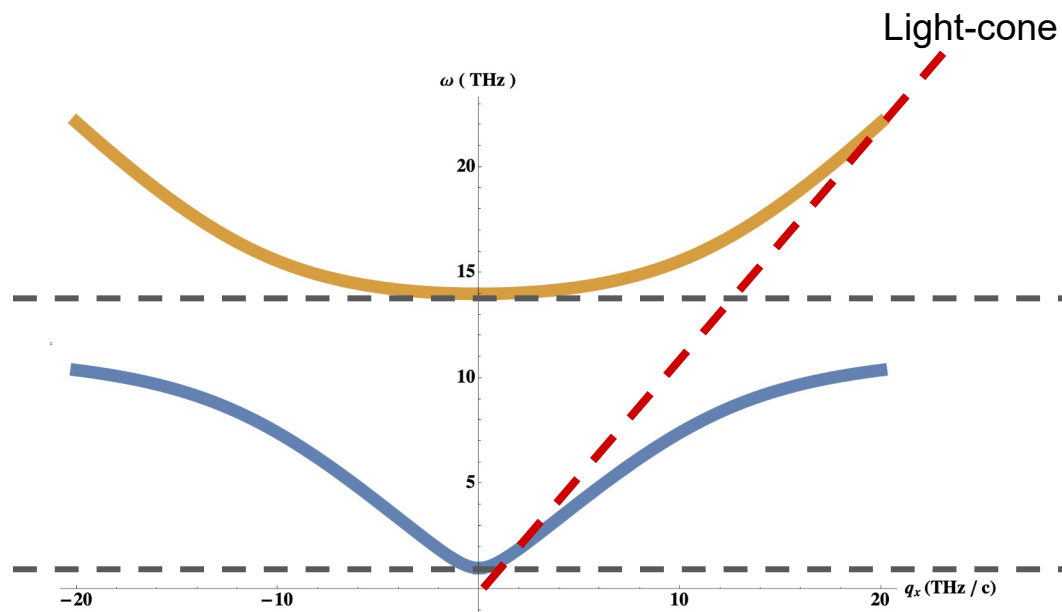
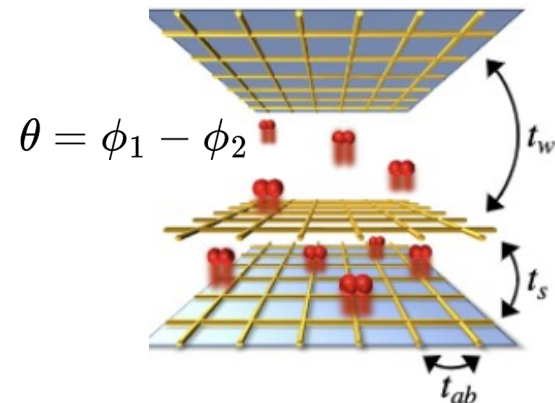
# Collective modes of phase dynamics:



$$\omega_s^2 \approx t_s |\psi_i|^2 \langle \cos(\theta) \rangle$$

$$\omega_w^2 \approx t_w |\psi_i|^2 \langle \cos(\theta) \rangle$$

# Collective modes of phase dynamics:



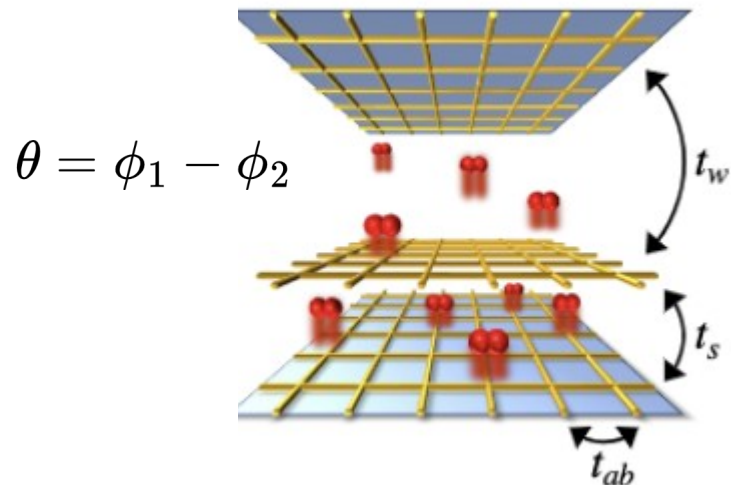
$$\omega_s^2 \approx t_s |\psi_i|^2 \langle \cos(\theta) \rangle$$

$$\omega_w^2 \approx t_w |\psi_i|^2 \langle \cos(\theta) \rangle$$

# Josephson plasmons:

Josephson current:

$$j_z = J_c \sin(\theta)$$



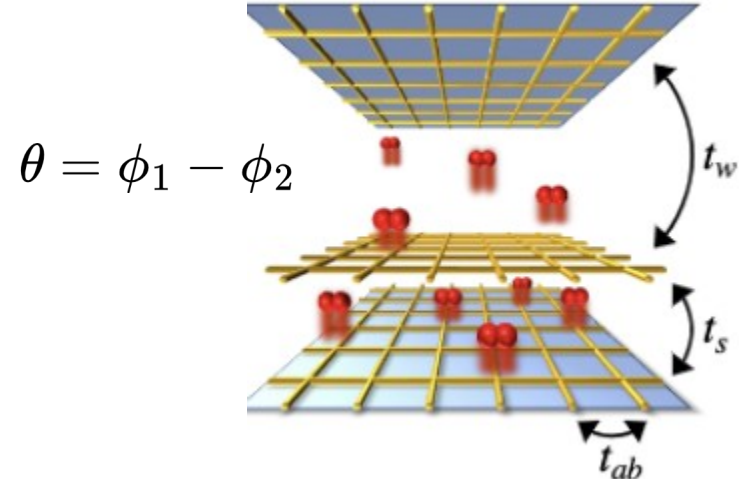
# Josephson plasmons:

Josephson current:

$$j_z = J_c \sin(\theta)$$

Sine-gordon model of a single Josephson layer:

$$\partial_t^2 \theta + \gamma \partial_t \theta + c^2 \partial_x^2 \theta + J_c \sin(\theta) = \lambda E(t)$$



# Josephson plasmons:

Josephson current:

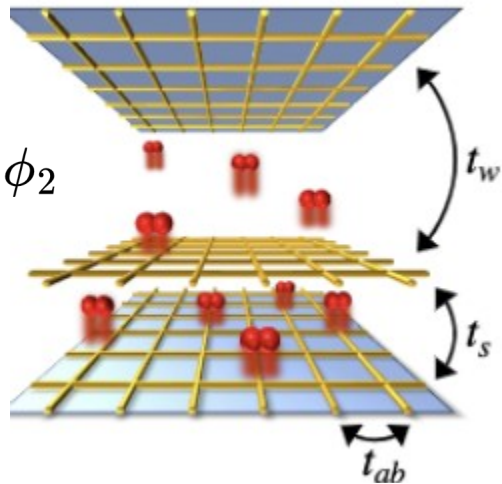
$$j_z = J_c \sin(\theta)$$

Source of strong non-linearity

Sine-gordon model of a single Josephson layer:

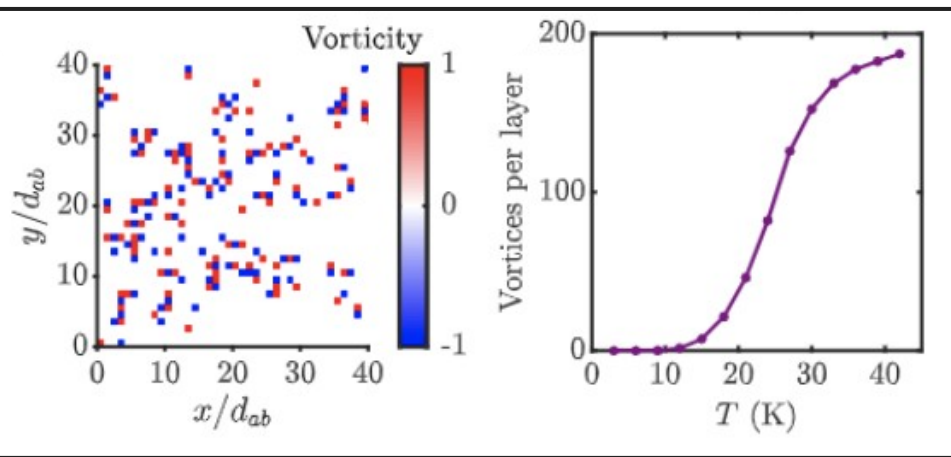
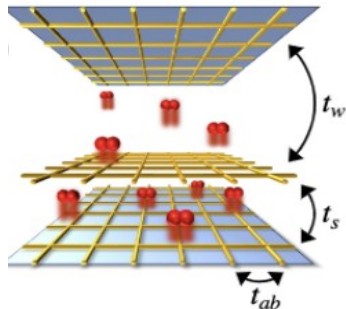
$$\partial_t^2 \theta + \gamma \partial_t \theta + c^2 \partial_x^2 \theta + J_c \sin(\theta) = \lambda E(t)$$

$$\theta = \phi_1 - \phi_2$$

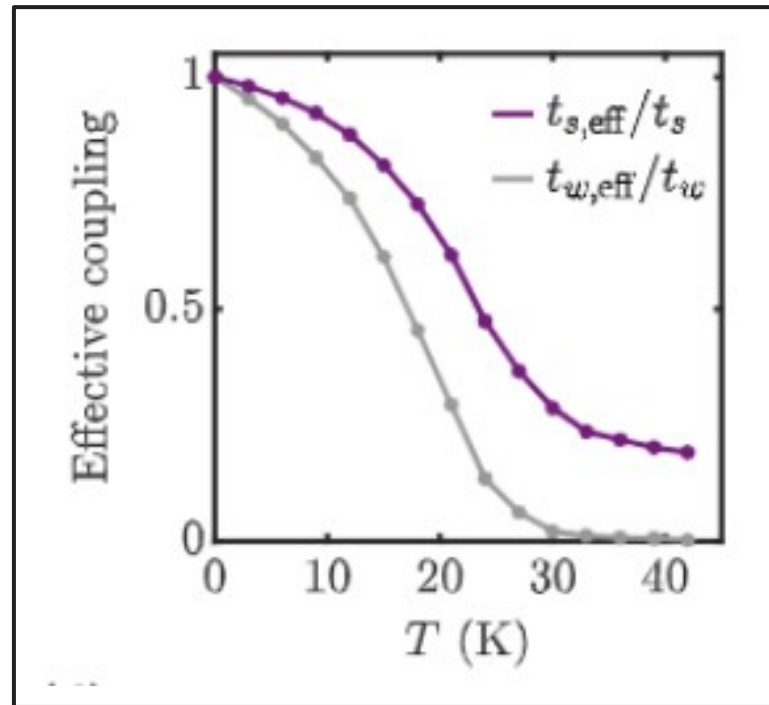




# Results:



Pancake vortices proliferate around 25 K.

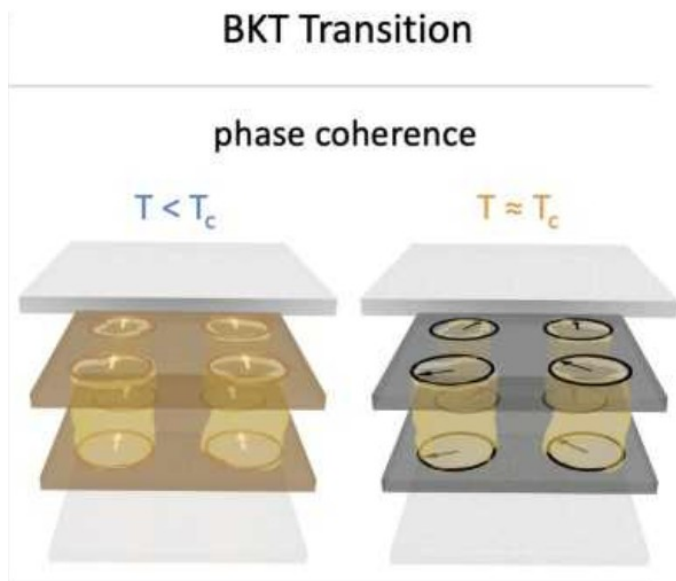


$$t_{w,eff} = t_w \langle \cos(\theta) \rangle$$

$$t_{s,eff} = t_s \langle \cos(\theta) \rangle$$

# Intrabilayer superconducting correlations:

**Claim:** Short range coherence in 3D anisotropic XY model **sufficient** to explain the plethora of nonlinear responses.



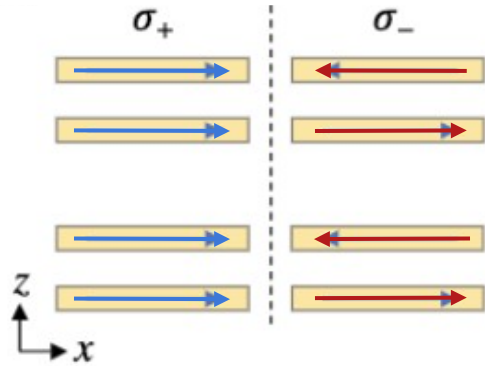
Long range order is lost:

$$\langle \psi^+(x) \psi(x') \rangle \sim |\psi(x)|^2 \langle e^{i\phi(x) - i\phi(x')} \rangle_{XY} = |\psi(x)|^2 e^{-x/\xi}$$

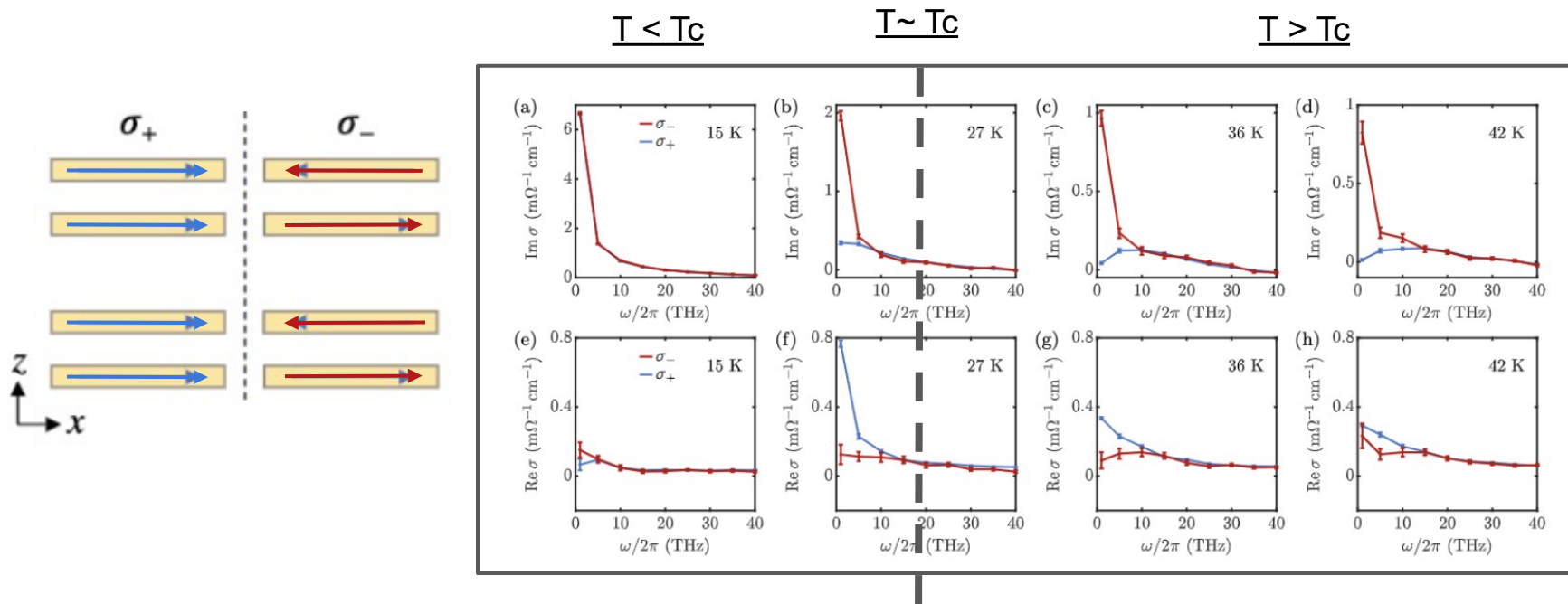
Locally strong Josephson nonlinearity:

$$\langle J_c \cos(\theta(x)) \rangle \neq 0$$

# Conductivity in the pseudogap:

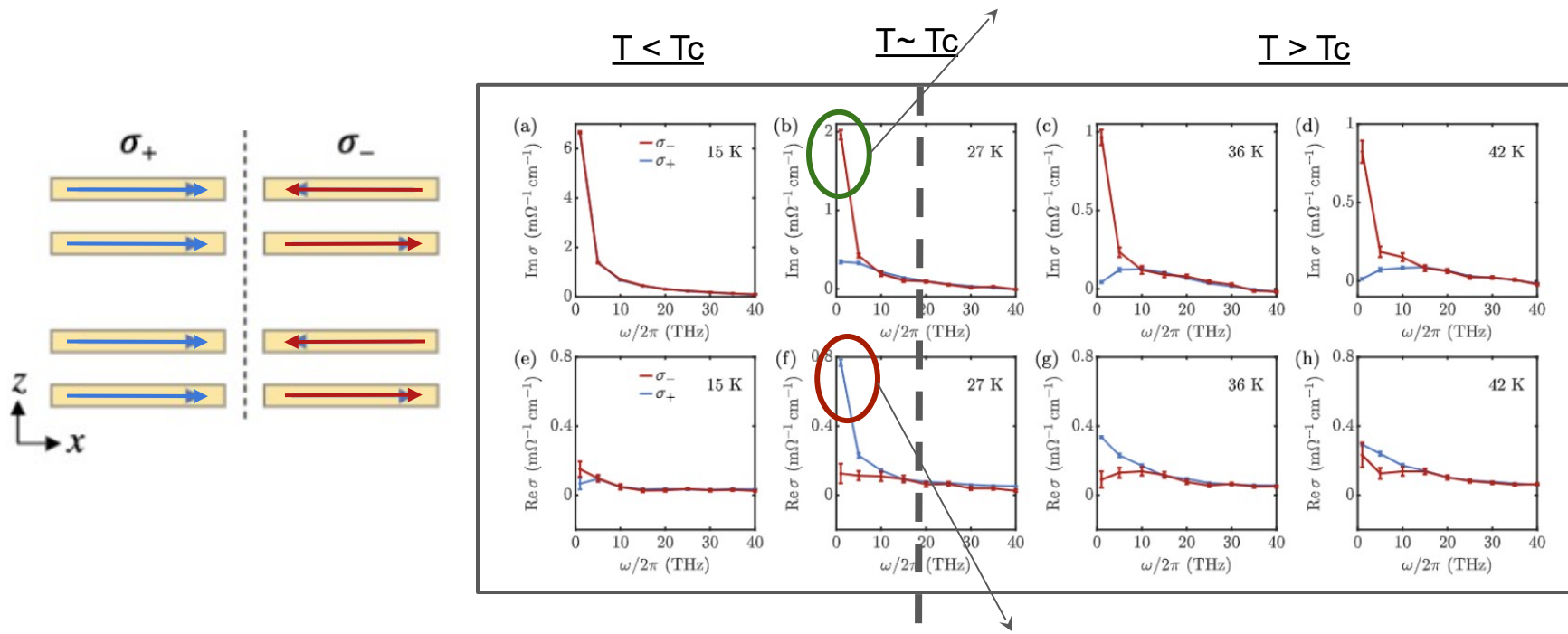


# Conductivity in the pseudogap:



# Conductivity in the pseudogap:

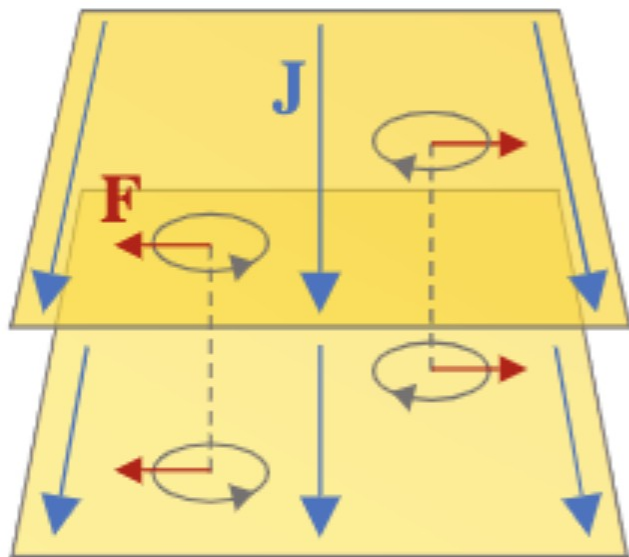
Counterflow supercurrent above  $T_c$ !!!



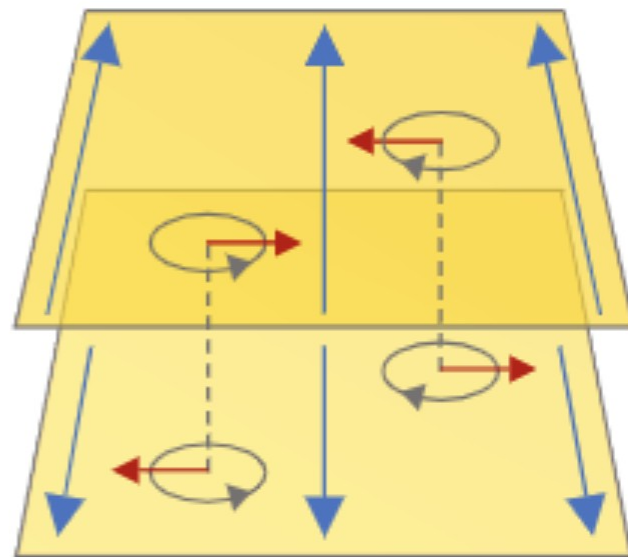
Resistive transition for total current.

# Origin of counterflow superconductivity

(a)



(b)



# Collaborators:

## Numerical simulations:



Guido Homann

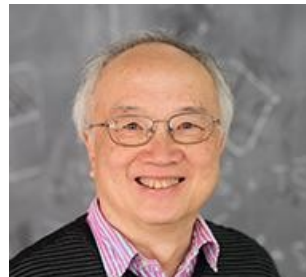


Ludwig Mathey

## Theory:

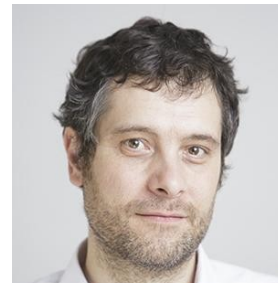


Eugene Demler



Patrick Lee

## Experiments:



Andrea Cavalleri

**Thank you !**